# dynPARTIX - A Dynamic Programming Reasoner for Abstract Argumentation<sup>\$</sup>

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### Motivation

- Increasing interest for reasoning in argumentation frameworks (AFs).
- Most reasoning tasks are highly computationally intractable.
- As AFs can be considered as graphs there is broad range of graph parameters we can consider to identify tractable fragments.
- The popular graph parameter tree-width allows for so called fixed-parameter tractable algorithms [Dunne, 2007; Dvořák et al., 2010].

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## Fixed-Parameter Tractability

- Often computational costs primarily depend on some problem parameters rather than on the mere size of the instances.
- Many hard problems become tractable if some problem parameter is fixed or bounded by a fixed constant.
- In the arena of graphs an important parameter is tree-width, which measures the "tree-likeness" of a graph. The tree-width has served as the key to many fixed-parameter tractability (FPT) results.

# Argumentation Frameworks

### Definition

An argumentation framework (AF) is a pair (A, R) where

- A is a set of arguments
- $R \subseteq A \times A$  is a relation representing "attacks"

### Example

$$F = (\{a, b, c, d\}, \{(a, b), (b, a), (a, c), (b, c), (c, d)\})$$



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# Argumentation Semantics

### **Conflict-Free Sets**

Given an AF F = (A, R). A set  $S \subseteq A$  is conflict-free in F, if, for each  $a, b \in S$ ,  $(a, b) \notin R$ .



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# Argumentation Semantics (ctd.)

### Admissible Sets

Given an AF F = (A, R). A set  $S \subseteq A$  is admissible in F, if

- S is conflict-free in F
- each  $a \in S$  is defended by S in F
  - a ∈ A is defended by S in F, if for each b ∈ A with (b, a) ∈ R, there exists a c ∈ S, such that (c, b) ∈ R.



# Argumentation Semantics (ctd.)

### Preferred Extensions

Given an AF F = (A, R). A set  $S \subseteq A$  is a preferred extension of F, if

- S is admissible in F
- for each  $T \subseteq A$  admissible in  $F, S \not\subset T$



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### Reasoning Problems

#### Credulous Acceptance

Given an AF F = (A, R) and an argument  $x \in A$ . Is x in at least one preferred extension ?

For credulous acceptance it suffices to consider admissible extensions.

### Skeptical Acceptance

Given an AF F = (A, R) and an argument  $x \in A$ . Is x in every preferred extension ?

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### Credulous Acceptance

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#### Complexity:

- The credulous acceptance problem is NP-complete.
- The skeptical acceptance problem is  $\Pi_2^p$ -complete.

# Tree-Decomposition

### Argumentation Framework



### Properties

For an AF F = (A, R):

- Each argument a ∈ A and each attack (b, c) ∈ R is contained in at least one bag
- Bags containing the same argument are connected

### **Tree-Decomposition**



# Tree-Decomposition

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**Tree-Decomposition** 



A Dynamic Programming Reasoner for Abstract Argumentation

## Tree-Width

### Width

The width of a tree-decomposition is the size of the largest bag - 1.

### Tree-Width

The tree-width of an AF is the minimum width over all possible tree-decompositions.

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# Dynamic Programming

#### **Basic Ideas:**

- Compute locally admissible / preferred sets for each bag with a bottom-up algorithm on the tree-decomposition
  - For each bag t we only store information about arguments in  $X_t$
  - The information about the "forgotten" arguments is implicitly encoded
- The results for the entire problem can be read from the root

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#### Theorem

Given an AF F = (A, R) of tree-width w and an argument  $a \in A$ , the DP-algorithm decides if x is accepted in time  $O(f(w) \cdot |F|)$ .

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### Theorem

Given an AF F = (A, R) of tree-width w and an argument  $a \in A$ , the DP-algorithm decides if x is accepted in time  $O(f(w) \cdot |F|)$ .

For details see [Dvořák, Pichler and Woltran KR'10].

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### Implementation

Our implementation builds on the SHARP<sup>1</sup> framework.

- SHARP offers ready-to-use implementations of various tree decomposition heuristics and
- helper methods for the Preprocessing and Dynamic Algorithm steps.
- It provides normalized tree decompositions, i.e. there are just four specific types of nodes.
- To implement our algorithms we just have to provide the methods and data structures for these four node types.



# Preliminary Experiments

We compare dynPARTIX with ASPARTIX<sup>2</sup>, one of the most efficient tools for abstract argumentation, on instances of low tree-width.

Test system: Intel®CoreTM 2 CPU 6300@1.86GHz SUSE Linux version 2.6.27.48

#### Test instances:

We randomly generated 4800 AFs varying the number of arguments; the tree-width; and the number of attacks. (To ensure that AFs are of a certain tree-width we used random grid-structured AFs.)

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<sup>&</sup>lt;sup>2</sup>www.dbai.tuwien.ac.at/research/project/argumentation/systempage/

# Experimental Results for Credulous Acceptance



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# Experimental Results for Skeptical Acceptance



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### Conclusion

- We presented dynPARTIX, a implementation of fixed-parameter tractable algorithms w.r.t. tree-width for
  - Credulous Reasoning
  - Skeptical Reasoning
  - Counting Extensions
  - Enumerating Extensions
- The techniques presented for preferred semantics are prototypical, i.e. can be easily applied to several other semantics.
- We provided preliminary experiments that underpin that our DP-algorithms pay off on instances of low tree-width.

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